## A Simple Model of Dynamic Energy Exchange Between a Sailplane and Vertical Air Currents.

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In the paper "Energy Exchange Between a Sailplane and Moving Air Masses..." by W. Gorisch, presented at the XV OSTIV Congress, the principles of optimal choice of airspeed and normal accelerations for a non-stationary dolphin-mode flight were given. In addition, the author's paper "Some Problems of the Dolphin-Mode Flight Technique" presented at the XVI OSTIV Congress concerned, in part, the same<br>problem. (Also see "Technical Soaring", Vol. VI, No. 3, March 1981 for a related paper "Energy Gain in Pitching Maneuvers" by W. Gorisch.)

The use of dynamic speed changes when flying through areas of vertical currents is aimed at increase of power transferred from the atmosphere to the sailplane. This power may be determined on the basis of a fundamental relation of mechanics stating that the derivative with respect to time of the total mechanical energy of a rigid body is given by the product of the velocity and the component in the velocity direction of the forces affecting the velocity in an inertial co-ordinate system.

The formula for the power transferred from the atmosphere to the sailplane flying through a vertical air current of constant velocity w<sub>atm</sub> was given by Gorisch<sup>1</sup>

 $E' = \frac{dE}{dt} = \overrightarrow{[L + D]} \overrightarrow{[V + w_{atm}]}$  $[1]$  $=$  Lw<sub>atu</sub>cosy - DV

where  $\varphi$  is the angle between lift  $L$  and air velocity vector  $w_{\text{atm}}$ . (Note that, by definition, drag is parallel to velocity and lift is orthogonal to

velocity. Since we are only interested

in vertical motion of the atmosphere Watm and V are orthogonal and lift and Watm are approximately parallel.)

The first term of the right side of this equation is the power transferred from the atmosphere to an ideal sailplane (with zero drag) and the second term is the power lost due to the aerodynamic drag.

Since both terms depend on the aerodynamic force which can be represented by an appropriate g-number, the rate of energy transfer must depend strongly on the g-loading; thus, an optimal value of load factor nopt corresponding with the maximum of power transferred from the atmosphere to the sailplane can be calculated. The higher gliding ratio of the sailplane at a given airspeed, the lower contribution of the equation's second term and the higher value of nopt. The same effect is to increase the effective intensity of the updraft  $w_{\text{atm}}$  .  $\cos\varphi$  which influences the first term of formula [1] and results in the increase of the optimum value of the load factor n<sub>opt</sub>. It seems, however, that this simple - from the point of view of mechanics - reasoning is not readily understandable by means of widely known physical terms such as potential and kinetic energy. At the same time it is obvious that the usefulness of dynamic controlling of the sailplane in dolphin-mode flight through vertical air currents for additional energy gain must be explained also to pilots having poor mathematical background. It is possible only on the basis of simple and easily understandable physical models.

For better presentation of the problem let us analyze the case of an ideal

sailplane in a level flight at the airspeed V and encountering an updraft having a velocity  $w_{\text{atm}}$ . Thus,  $\varphi = 0$ :

$$
E' = Lw_{atm} \tag{2}
$$

and therefore the power transferred from the atmosphere is proportional to the lift L.

If the pilot does not perform a dynamic pull-out then

 $L = m.g \longrightarrow E' = m.g.watm$ 

and the power absorbed from the atmosphere transfers in time At into the potential energy increment

 $\Delta E_{\text{pot}}$  = mgw<sub>atm</sub>.  $\Delta t$  = m.g. $\Delta h$  $\left[\begin{matrix}3\end{matrix}\right]$ 

which is physically evident.

For precision it must be mentioned that a "step" increment of the sailplane's kinetic energy

$$
\Delta E_{\text{kin}} = \frac{m \cdot w_{\text{atm}}^2}{2}
$$

proportional to the square of the velocity of transportation watm occurs at the moment of entry into the updraft.

Let us now examine the pull-out maneuver. In a co-ordinate system moving together with the vertical air current [Fig. 1], a sudden change of angle of attack induces a lift increment  $\Delta L$  and consequently a curvature of the flight path. In time  $\Delta t$  the sailplane moves from point 1 to point 2.

Following formula [2], the additional power absorbed from the atmosphere

$$
E' = \Delta L \cdot w_{\text{atm}} \cos \varphi
$$
 [4]

and the additional energy increment at point 2, due to dynamic maneuvering:

$$
\Delta E = \Delta L . w_{atm}. \cos \theta_{mean} . \Delta t
$$
 [5]

Let us now try to find the physical form of this additional energy.

The potential energy increment m.g  $\Delta z$ due to the fact that point 2 lies higher than point 1 is of no importance because it is compensated by equivalent drop of kinetic energy due to the loss of the sailplane's airspeed; in such a case we observe only a change of the form of

energy and consequently no gain of total energy occurs. Thus, we can neglect this potential energy increment assuming simultaneously that the airspeed on the way from 1 to 2 remains constant.

Let us now seek the additional energy increase, evaluated by means of formula [5] in the form of kinetic energy. For this purpose we must decompose the airspeed at point 2 into horizontal and vertical components [Fig. 1]. Taking into account the transportation velocity of co-ordinate system w<sub>atm</sub>, the total kinetic energy of the sailplane at point  $2:$ 

$$
E_{kin} = \frac{m(v\cos\theta)^2}{2} = \frac{m(v\sin\theta + w_{atm})^2}{2}
$$

$$
= \frac{mV^2}{2} = \frac{m\omega^2 a t m}{2} + m v_{atm} . V \sin\theta
$$
 [6]

The first two terms of the right side of this equation represent the kinetic energy of the sailplane in straight flight, i.e. at point 1, while the third term represents an amount of additional energy due to the curvature of the flight path in a velocity of transportation field. The formula [6] shows clearly that necessary conditions for the occurance of the additional kinetic energy are two factors - flight path curvature angle  $f$  and velocity of

tranportation  $w_{a+m}$ .<br>Now it must still be proved that the power required for the energy gain is equal to the power absorbed from the atmosphere according to formula  $[4]$ :

$$
E' = \frac{d}{dt} (mw_{atm} \cdot V \sin f)
$$
  
= m. w<sub>atm</sub>V $\frac{d\phi}{dt}$ cos $\theta$  =  $\Delta L . w_{atm}$ .cos $\phi$ 

since  $mV \frac{d\phi}{d\bar{t}} = \Delta L$ 

Let us now sum up the above considerations as follows: the positive or negative energy exchange between atmosphere and a sailplane, resulting from its dynamic longitudinal maneuvers during flight through vertical air currents, can be easily explained to a pilot as an additional amount (positive or negative) of kinetic energy. This is due to the fact that the vertical component of the sailplane's velocity.







Fig. 2 Flight path of a sailplane performing a dynamic maneuver in an area of constant vertical velocity.

with respect to the earth, is a sum of<br>the vertical component of the sailplane's airspeed and the velocity of transportation (velocity of the air current). The kinetic energy of the resultant motion is proportional to the square of this sum and therefore is higher than the sum of the energy of both separate motions.

In the same manner, we can explain a formula given by Gorisch concerning the sailplane's energy gain in a flight through an area of constant vertical velocity  $w_{\text{atm}}$  [Fig. 2].

 $\Delta E$  = m.w<sub>atm</sub> $\Delta z$ <sup>1</sup> + mg(w<sub>atm</sub> - w<sub>mean</sub>)  $\Delta t$  [7]

where the first term of the right side

is the additional energy increment due to the dynamic maneuver.

Also, conclusions drawn by the author [Ref. 2] concerning optimization of non-stationary dolphin-mode flight can be made perceptible to the pilots when this simple model of dynamic energy exchange is used.

## **REFERENCES**

1. Gorisch, W.: "Energy Exchange Between a Sailplane...," Aero Revue, 11/1976 8 12/1976. 2. Sandauer, J.: "Some Problems of the

Dolphin-Mode Flight Technique," Aero Revue, 1/1981.